

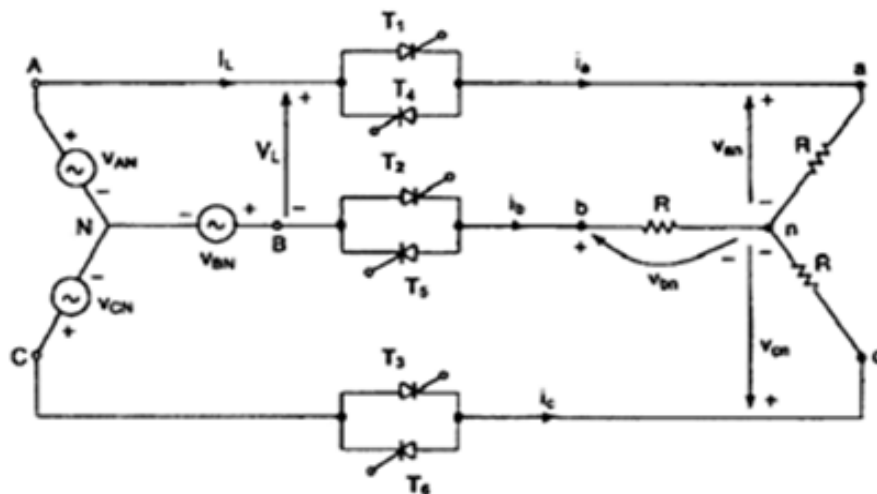
# 12. Three-phase AC Controllers

## Fully controlled Three- phase AC controller

A 3-phase full –wave fully controlled AC controller is shown in Fig.1. With a star connected resistive load.

The firing sequence of thyristors is T1,T6,T2,T4,T3,T5

Fig.1



- For current to flow it is necessary to trigger at least two thyristors at a time.
- If we define the instantaneous input phase voltages as:

$$v_{an} = V_m \sin \omega t$$

$$v_{bn} = V_m \sin (\omega t - 2\pi / 3)$$

$$v_{cn} = V_m \sin (\omega t - 4\pi / 3)$$

- The instantaneous input line voltages are

$$v_{ab} = \sqrt{3} v_{an} = \sqrt{3} v_m \sin (\omega t + \pi/6)$$

$$v_{bc} = \sqrt{3} v_{bn} = \sqrt{3} v_m \sin (\omega t - \pi/2)$$

$$v_{ca} = \sqrt{3} v_{cn} = \sqrt{3} v_m \sin (\omega t - 7\pi/6)$$

The waveforms the input voltages, conduction angles of thyristors and output phase voltages are shown in Fig.2 for  $\alpha = 30^\circ$

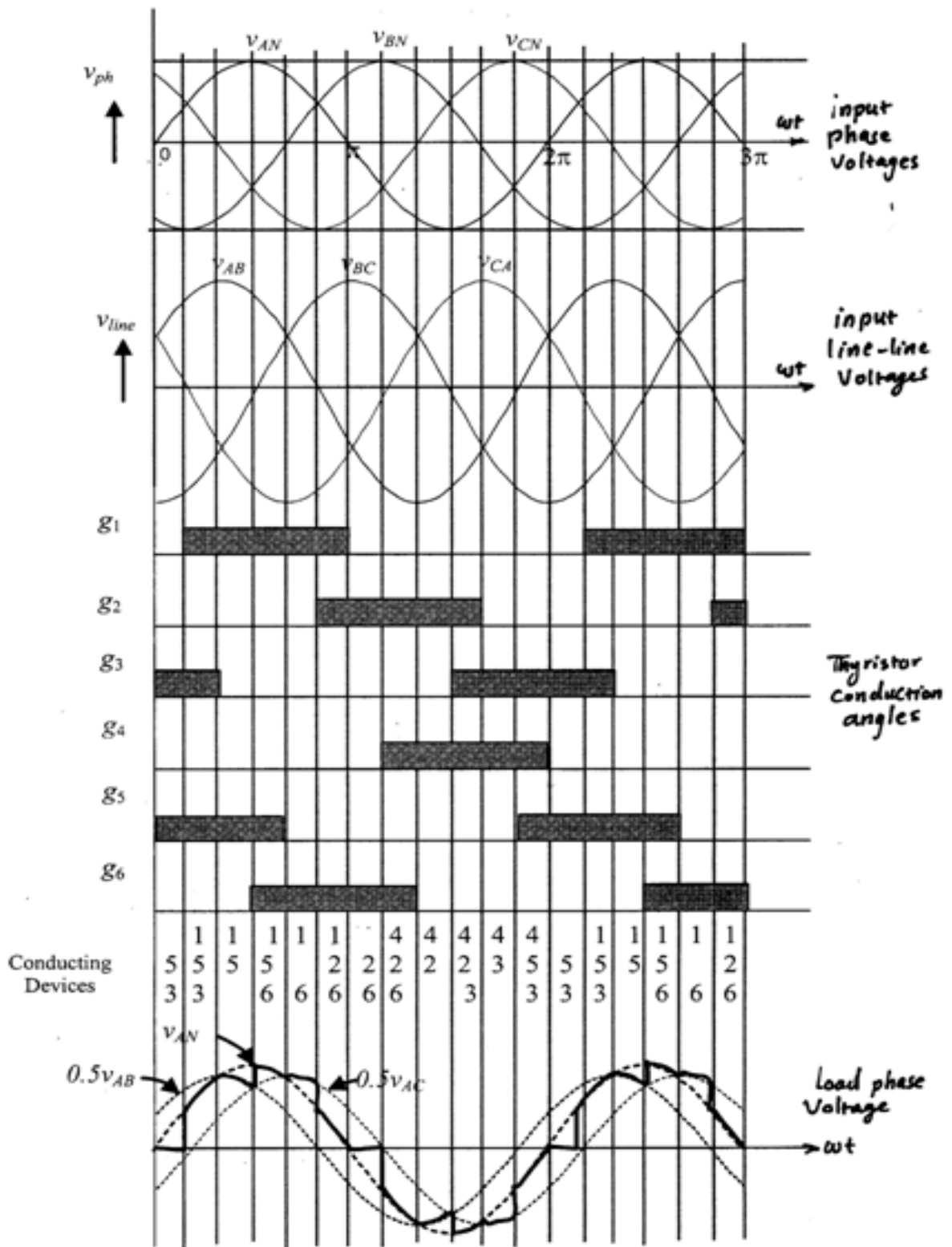


Fig.2 Waveforms

For complete control of the thyristors using the triggering pattern shown each thyristor must be triggered by two separated by 60 degree in time.

Hence we have generally three distinct ranges of firing angle:

- |              |                                       |
|--------------|---------------------------------------|
| 1- Range (1) | $0^\circ \leq \alpha < 60^\circ$      |
| 2- Range (2) | $60^\circ \leq \alpha < 90^\circ$     |
| 3- Range (3) | $90^\circ \leq \alpha \leq 150^\circ$ |

Similar to half wave controllers the expression for the R.M.S output phase voltage depends on the range of firing angles.

The R.M.S output voltage for a Y- connection loads are found to be:

1- For  $0^\circ \leq \alpha < 60^\circ$

$$V_o = \sqrt{3} V_m \sqrt{\frac{1}{\pi} \left( \frac{\pi}{6} - \frac{\alpha}{4} + \frac{\sin 2\alpha}{8} \right)}$$

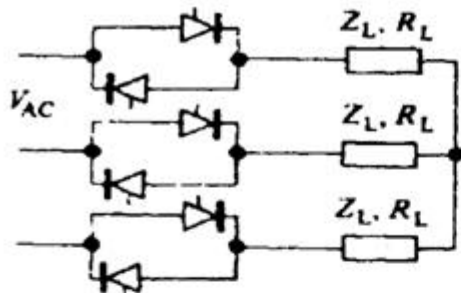
2- For  $60^\circ \leq \alpha < 90^\circ$

$$V_o = \sqrt{3} V_m \sqrt{\frac{1}{\pi} \left( \frac{\pi}{12} - \frac{3 \sin 2\alpha}{6} + \frac{\sqrt{3} \cos 2\alpha}{16} \right)}$$

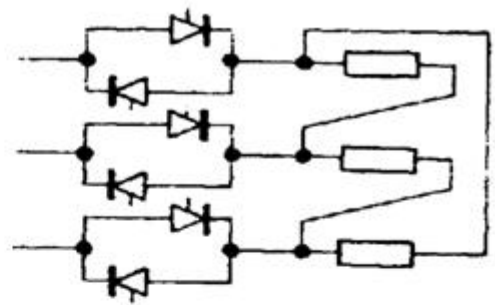
3- For  $90^\circ \leq \alpha \leq 150^\circ$

$$V_o = \sqrt{3} V_m \sqrt{\frac{1}{\pi} \left( \frac{5\pi}{24} - \frac{\alpha}{4} + \frac{\sin 2\alpha}{16} + \frac{\sqrt{3} \cos 2\alpha}{16} \right)}$$

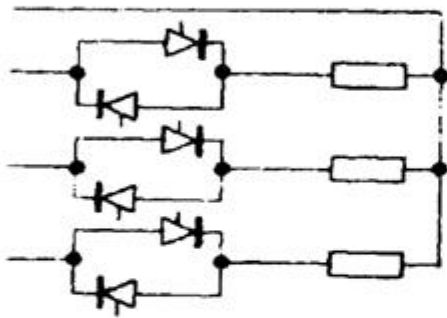
## Other types of 3-Phase AC controllers



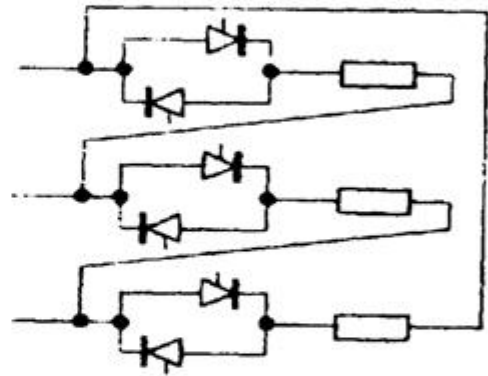
A 3-wire star load



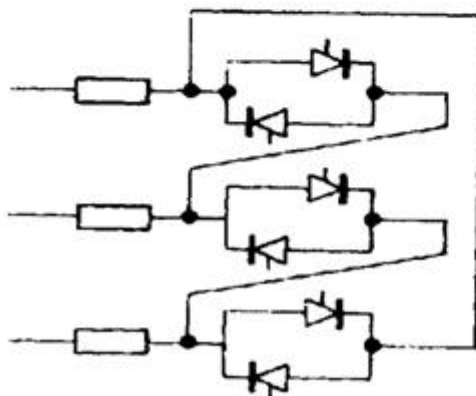
B 3-wire delta load



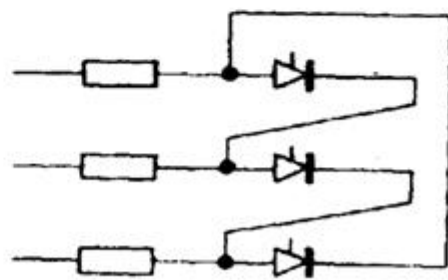
C 4-wire star load



D 3-wire delta controller



E Control in delta



F Half-wave delta control

## Applications:

- Phase controlled systems are used for controlling the speed of induction motor is shown in Fig.4:

Fig.4 (a) Open loop  
Speed control of induction  
Motor using 3-phase  
AC voltage controller

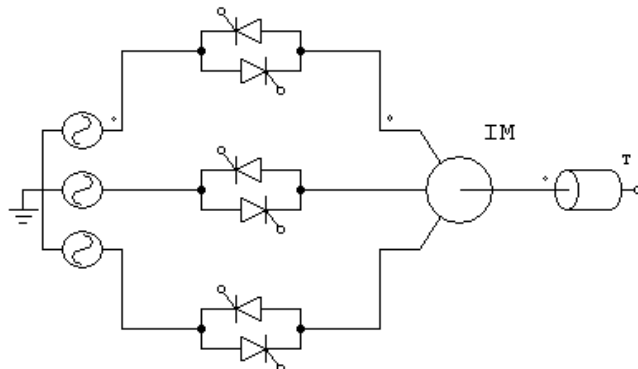
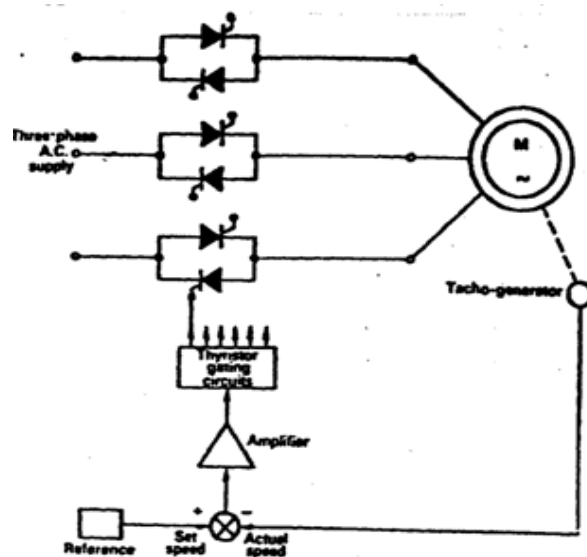
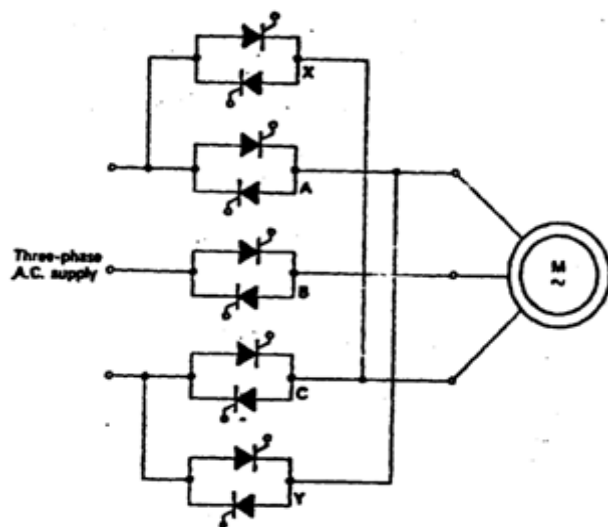


Fig.4(b) Closed loop system  
for inductive motor speed  
control using 3-phase  
AC voltage controller



- If a reversible speed control system is used the line must be change cross connected system Fig.5:

Fig.5 Thyristor configuration  
of a reversible speed induction  
drive.



**Example:**

The three phase bidirectional controller in Fig.6 supplies a Y- connected resistive load of  $R = 10 \Omega$  and line to line voltage is 208V RMS and  $f=60$  Hz. For the delay  $\alpha=\pi/6$  determine

- The output power
- The input power factor PF
- Give one application of such a converter

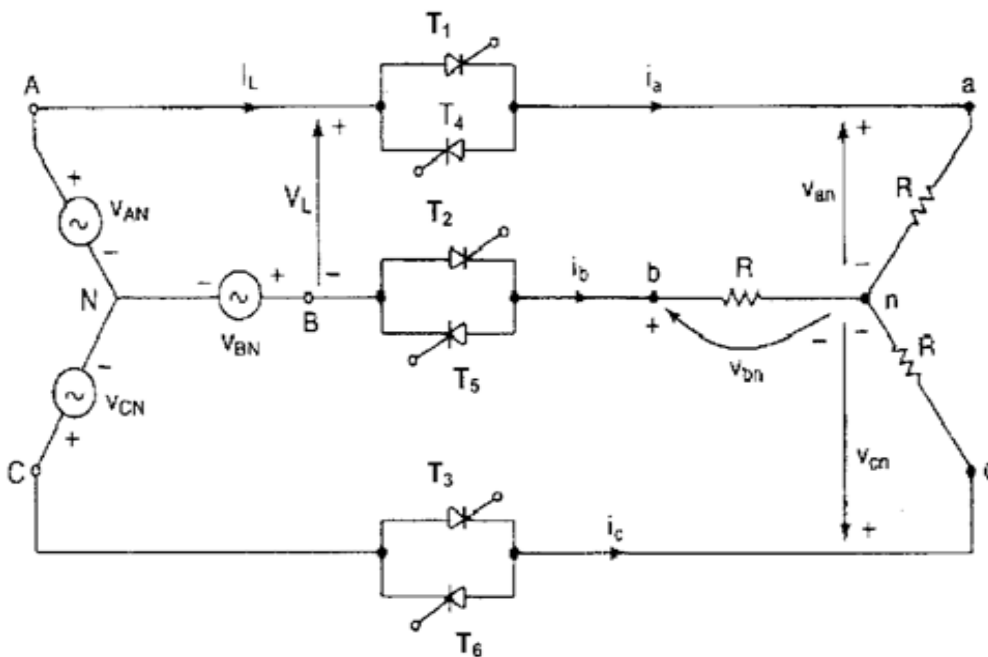


Fig.6

>>> NOT THAT

For  $0^\circ \leq \alpha < 60^\circ$

$$V_o = \sqrt{3} V_m \sqrt{\frac{1}{\pi} \left( \frac{\pi}{6} - \frac{\alpha}{4} + \frac{\sin 2\alpha}{8} \right)}$$

For  $60^\circ \leq \alpha < 90^\circ$

$$V_o = \sqrt{3} V_m \sqrt{\frac{1}{\pi} \left( \frac{\pi}{12} - \frac{3 \sin 2\alpha}{6} + \frac{\sqrt{3} \cos 2\alpha}{16} \right)}$$

For  $90^\circ \leq \alpha \leq 150^\circ$

$$V_o = \sqrt{3} V_m \sqrt{\frac{1}{\pi} \left( \frac{5\pi}{24} - \frac{\alpha}{4} + \frac{\sin 2\alpha}{16} + \frac{\sqrt{3} \cos 2\alpha}{16} \right)}$$

**Solution:**

**(a)** For  $0^\circ \leq \alpha < 60^\circ$

$$V_o = \sqrt{3} V_m \sqrt{\frac{1}{\pi} \left( \frac{\pi}{6} - \frac{\alpha}{4} + \frac{\sin 2\alpha}{8} \right)} = 117.38V$$

$$I_o = \frac{V_o}{R} = \frac{117.38}{10} = 11.74A$$

$$P_o = 3I_o^2 R = 3 * (11.74)^2 * 10 = 4134W$$

**(b)** Since the load is Y-connection the phase current. Thus the input volt-ampere power is

$$S = 3V_s I_o = 3 * 120 * 11.74 = 4226VA$$

$$PF = \frac{P_o}{S} = \frac{4134}{4226} = 0.978 \text{lagging}$$

**(c)** One application of three-phase AC regulator is in electric oven control or induction motor speed control.