

9. BODE PLOT FROM A TRANSFER FUNCTION

AIM:

To obtain bode plot for a given transfer function of the system using MATLAB.

APPARATUS:

Software: MATLAB

THEORY:

Bode computes the magnitude and phase of the frequency response of LTI models. When invoked without left-side arguments, bode produces a Bode plot on the screen. The magnitude is plotted in decibels (dB), and the phase in degrees. The decibel calculation for mag is computed as $20\log_{10}(|H(j\omega)|)$, where $H(j\omega)$ is the system's frequency response. Bode plots are used to analyze system properties such as the gain margin, phase margin, DC gain, bandwidth, disturbance rejection, and stability.

Bode Calculations Gain

The magnitude of the transfer function T is defined as:

$$|T(j\omega)| = \sqrt{R^2 + X^2}$$

However, it is frequently difficult to transition a function that is in "numerator/denominator" form to "real+imaginary" form. Luckily, our decibel calculation comes in handy. Let's say we have a frequency response defined as a fraction with numerator and denominator polynomials defined as:

$$T(j\omega) = \frac{\prod_n |j\omega + z_n|}{\prod_m |j\omega + p_m|}$$

If we convert both sides to decibels, the logarithms from the decibel calculations convert multiplication of the arguments into additions, and the divisions into subtractions:

$$\text{Gain} = \sum_n 20\log(j\omega + z_n) - \sum_m 20\log(j\omega + p_m)$$

bode(sys) plots the Bode response of an arbitrary LTI model sys. This model can be continuous or discrete, and SISO or MIMO. In the MIMO case, bode produces an array of Bode plots, each plot showing the Bode response of one particular I/O channel. The frequency range is determined automatically based on the system poles and zeros.

bode(sys,w) explicitly specifies the frequency range or frequency points to be used for the plot. To focus on a particular frequency interval [wmin,wmax], set w = {wmin,wmax}. To use particular frequency points, set w to the vector of desired frequencies. Use logspace to generate logarithmically spaced frequency vectors. All frequencies should be specified in radians/sec.

bode(sys1,sys2,...,sysN) or bode(sys1,sys2,...,sysN,w) plots the Bode responses of several LTI models on a single figure. All systems must have the same number of inputs and outputs, but may otherwise be a mix of continuous and discrete systems. This syntax is useful to compare the Bode responses of multiple systems.

bode(sys1,'PlotStyle1',...,sysN,'PlotStyleN') specifies which color, linestyle, and/or marker should be used to plot each system. For example,

```
bode(sys1,'r--',sys2,'gx')
```

uses red dashed lines for the first system sys1 and green 'x' markers for the second system sys2.

When invoked with left-side arguments

```
[mag,phase,w] = bode(sys)
```

```
[mag,phase] = bode(sys,w)
```

return the magnitude and phase (in degrees) of the frequency response at the frequencies w (in rad/sec). The outputs mag and phase are 3-D arrays with the frequency as the last dimension (see "Arguments" below for details). You can convert the magnitude to decibels by

```
magdb = 20*log10(mag)
```

MATLAB PROGRAM:

```
num=input('enter the numerator of the transfer function')
```

```
den=input('enter the denominator of the transfer function')
```

```
h=tf(num,den)
```

```
[gm pm wcp wcg]=margin(h)
```

```
bode(h)
```

PROCEDURE:

- Write the MATLAB program in the MATLAB editor.
- Then save and run the program.
- Give the required inputs.
- The syntax "bode(h)" solves the given input transfer function and gives the bode plot,
- where num,den are the numerator and denominator of the transfer function.
- Now plot the bode plot theoretically for the given transfer function and compare it with the plot obtained practically.

EXAMPLE:

Transfer function=

THEORETICAL CALCULATIONS:

enter the numerator of the transfer function

num =

enter the denominator of the transfer function

den =

Transfer function:

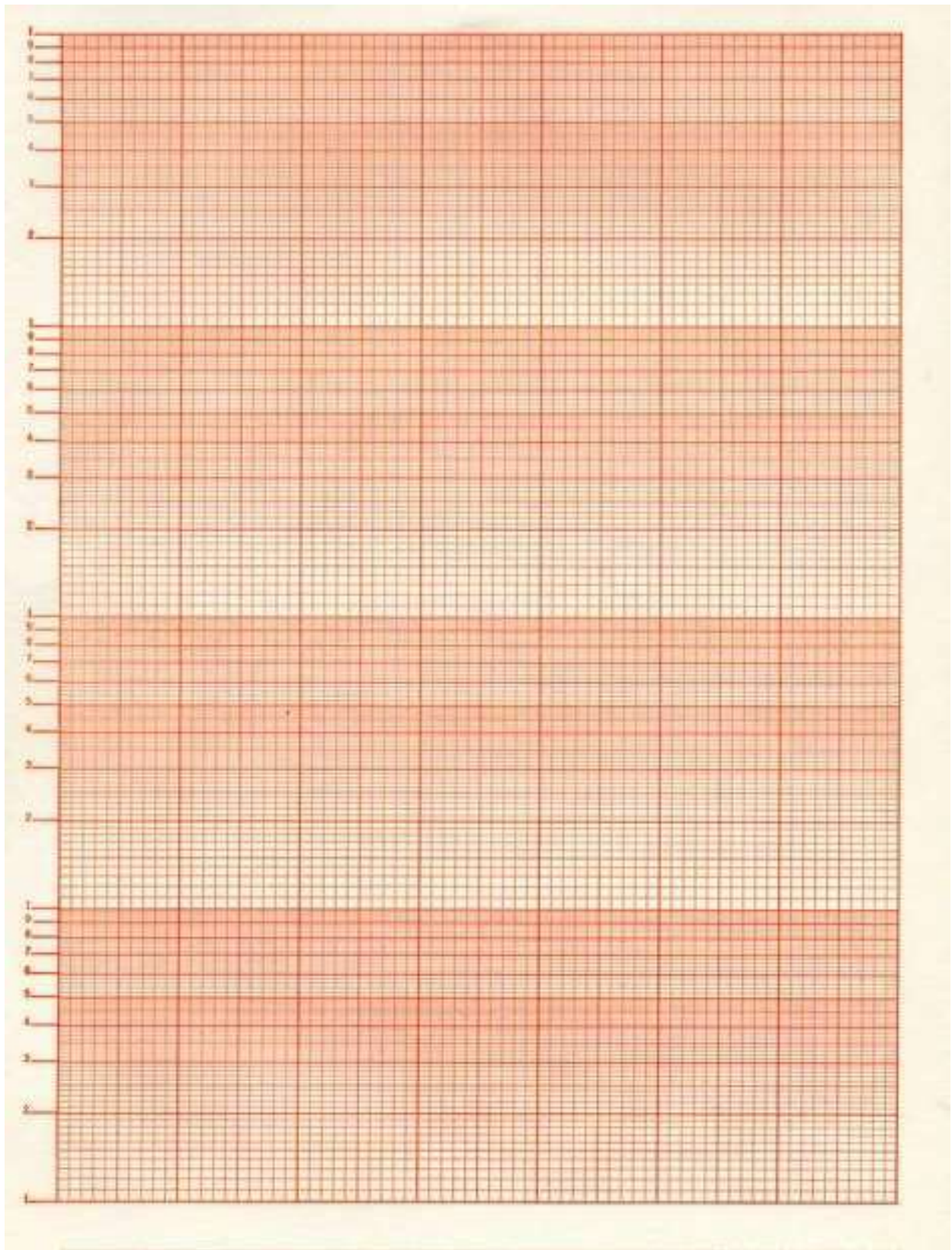
gm =

pm =

wcp =

wcg =

GRAPH



RESULT: